### Introduction to Analyzing Noise in Photodiode Amplifiers

### Presented By: S.E Nickols for the staff of Gen-Probe

# Nick's Background.

- Experience: Over 20 years of electronics/systems design, design analysis, design verification, product certification, manufacturing transfer, and vendor management. Have recent experience with medical device development. Have had involvement with design control, risk management and regulatory issues. (class II and III)
- **Industries:** Scientific, Semiconductor, and Medical.
- Interests: Projects requiring a multidisciplinary approach to solve a customer's problem.
- <u>Approach</u>: Team player. Quality Oriented. Process oriented. Customer oriented.
- What I Bring to table: Aside from technical skill and experience, "hind sight", a can do attitude, flexible, strong adaptation skills, open minded, here to make you money.

## **Presentation Contents**

### Photodiode Review

- Photo Detector Basics
- Noise Concepts Review
- Photodiode and Amplifier Noise Theory
- •Bandwidth and Stability Calculations
- •Transimpedance Amplifier Theoretical Noise Calculations
- •Transimpedance Amplifier Tina Spice Analysis
- •Transimpedance Measurement Example
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## **Photodiode Review**

#### **Introduction**

• Photodiodes convert light into current or voltage.

**Commonly Used Photodiode types:** 

- PN photodiode more wavelength selective (Solar cell)
- PIN photodiode wide spectral range (less selective) Most widely used.
- APD (Avalanche photodiode) sensitive to low light, fast





#### SPECTRAL RESPONSE

# **Basic Photodiode Physics**



#### **Principle of Operation:**

. - The P-layer material at the active surface and the N material at the substrate form a PN junction which operates as a photoelectric converter.

- When light strikes a photodiode, the electron within the crystal structure becomes stimulated. If the light energy is greater than the band gap energy Eg, the electrons are pulled up into the conduction band, leaving holes in their place in the valence band.

- These electron-hole pairs occur throughout the P-layer, depletion layer and N-layer materials. In the depletion layer the electric field accelerates these electrons toward the N-layer and the holes toward the P-layer.

- This results in a positive charge in the P-layer and a negative charge in the N-layer. If an external circuit is connected between the P- and N-layers, electrons will flow away from the N-layer, and holes will flow away from the P-layer toward the opposite respective electrodes.

## **Photodiode Circuit Model Basics**



 $\mathbf{r}_{\pmb{\varphi}}$  is the diode's flux responsivity

 $\boldsymbol{\varphi}_{\underline{a}}$  is the radiant flux energy in Watts

- $I_D$ : Diode Current
- C<sub>i</sub> : Junction capacitance

 $I_L = r_{\phi} \phi_e$ 

$$C_{j} = \frac{C_{j0}}{\sqrt{1 + \frac{V_{R}}{\phi_{B}}}}$$

 $C_{j0}$  is the photodiode capacitance at zero bia  $\phi_{B}$  is the built-in voltage of the diode junction

 $\rm V_{R}$  is the reverse bias voltage

- R<sub>sh</sub> : Shunt resistance
- R<sub>s</sub>: Series resistance
- I': Shunt resistance current
- $V_D$  : Diode Voltage
- I<sub>o</sub> : Output current
- V<sub>o</sub> : Output voltage

## Photodiode Basics Continued



Use left equivalent circuit, the output current is given as :

$$I_{o} \coloneqq I_{L} - I_{D} - I' = I_{L} - I_{S} \left( e^{\frac{eV_{D}}{kT}} - 1 \right) - I'$$

- I<sub>S</sub>: Photodiode reverse saturation curren
- e: electron charge
- k: Boltzmann's constant
- T: Absolute temperature of the photodioc

The open circuit voltage V<sub>oc</sub> is the output voltage when I<sub>0</sub> equals 0. Thus Voc becomes:



## **Photo Diode Properties**

#### Key Properties

The most important properties of photodiodes are:

- The <u>responsivity</u>, i.e., the photocurrent divided by optical power related to the quantum efficiency, dependent on the wavelength where h v is the photon energy,  $\eta$  is the quantum efficiency, and e the elementary charge. For example, a photodiode with 90% quantum efficiency at a wavelength of 800 nm, the responsivity would be  $\approx 0.58$  A/W The <u>quantum</u> <u>efficiency</u> of a photodiode is the fraction of the incident (or absorbed) photons which contribute to the photocurrent.
- The <u>active area</u>, i.e., the light-sensitive area
- The *maximum allowed photocurrent* (usually limited by saturation)
- The <u>dark current (in photoconductive mode, important for the detection of low light levels)</u>
- The speed, i.e. <u>response time</u>, related to the rise and fall time, often influenced by the capacitance.
- Notes:

Higher photocurrents are actually desirable for suppression of shot noise and thermal noise. Larger active areas (with diameters up to the order of 1 cm) allow for handling of larger beams and for much higher photocurrents, but at the expense of lower speed

The quantum efficiency of a photodiode can be very high – in some cases more than 95% – but varies significantly with wavelength. Apart from a high internal efficiency, a high quantum efficiency requires the suppression of reflections e.g. with an anti-reflection coating.

 $R = \eta \frac{e}{h\nu}$ 

## **Semiconductor Materials**

Commonly used photodiode materials are:

•<u>Silicon (Si):</u> low dark current, high <u>speed</u>, good sensitivity between roughly 400 and 1000 nm (best around 800– 900 nm) .

•<u>Germanium (Ge)</u>: high dark current, slow speed due to large parasitic capacity, good sensitivity between roughly 900 and 1600 nm (best around 1400–1500 nm).

•*Indium Gallium Arsenide Phosphide (InGaAsP):* expensive, low dark current, high speed, good sensitivity roughly between 1000 and 1350 nm (best around 1100–1300 nm).

•<u>Indium Gallium Arsenide (InGaAs)</u>: expensive, low dark current, high speed, good sensitivity roughly between 900 and 1700 nm (best around 1300–1600 nm) The indicated wavelength ranges can sometimes be substantially exceeded by models with extended spectral response.



## **Example Photodiode: "Advanced Photonix" PDB-C158**

#### ABSOLUTE MAXIMUM RATING (TA)= 23°C UNLESS OTHERWISE NOTED

SYMBOL	PARAMETER	MIN	MAX	UNITS
V <sub>BR</sub>	Reverse Voltage		50	V
T <sub>STG</sub>	Storage Temperature	-40	+100	°C
To	Operating Temperature -40 +80 °C		°C	
T <sub>S</sub> Soldering Temperature*			+260	°C

#### SPECTRAL RESPONSE



\* 1/16 inch from case for 3 seconds max.

#### ELECTRO-OPTICAL CHARACTERISTICS RATING (TA)= 23°C UNLESS OTHERWISE NOTED

							-
SYMBOL	CHARACTERISTIC	TEST CONDITIONS	MIN	TYP	MAX	UNITS	
I <sub>SC</sub>	Short Circuit Current	H = 100 fc, 2850 K	100	145		μΑ	
I <sub>D</sub>	Dark Current	V <sub>R</sub> = 10 V		2	30	nA	
Reh	Shunt Resistance	V <sub>P</sub> = 10 mV	100	150		MΩ	
CJ	Junction Capacitance	$V_{R} = 10 V, f = 1 MHz$		10	25	pF	
$\lambda$ range	Spectral Application Range	Spot Scan	400		1100	nm	
V <sub>BR</sub>	Breakdown Voltage	I = 10 μA	30	75		V	
NEP	Noise Equivalent Power	V <sub>R</sub> = 10V @ $\lambda$ = Peak		4.4x10 <sup>-14</sup>		W/ $\sqrt{_{\rm Hz}}$	
t <sub>r</sub>	Response Time	RL = 1KΩ,V <sub>R</sub> = 10 V		50		nS	
+				• •		-	4

\*\*Response time of 10% to 90% is specified at 660nm wavelength light.

#### Cj is not specified at Vr=0V.

Calling the manufacturer for this information, Cj=70pF for Vr=0V

## **PIN Diode Structure**



# **Photo Detector Basics**

**Basic Photodetector Circuit** 



## **Photo Voltaic Mode Amplifier**



# Photo Voltaic Mode Amplifier

Use Photovoltaic Mode:

 Where precision is more important then speed.

The lack of dark current removes an entire error term. The lower noise makes smaller measurements possible. The linear output makes calculations trivial.

# Photo Conductive Mode

**Negative Bias Circuit** 



+/- 10V, there is voltage across the diode.

## **Photo Conductive Mode Amplifier**

## **Use Photoconductive Mode:**

- Where speed is more important then precision. The voltage across the diode lowers it's capacitance. This allows faster amplifiers:
  - Less capacitance allows a faster amplifier while maintaining stability.

# **Noise Review**

## **Intrinsic Noise**

- Error Source
- Generated by circuit itself (not pickup)
- Calculate, Simulate, and Measure









## **Time Domain – White noise normal distribution**



# What is Spectral Density?



## Convert Spectral Density to RMS Convert RMS to Peak-to-Peak



## **Photodiode vs. Photo Amplifier Noise?**

- Noise is a key parameter in photodiode design
  - Wide bandwidth (integrate more noise)
  - Low signal levels (noise more critical)
- Photodiode amplifier noise is more complex
  - Parasitic capacitance and sensor capacitance
  - Poles and zeros
  - Gain peaking

## **Sources of Noise**



# **Photodiode Amplifier Noise Theory**

## **Photo-Diode Amp Noise Model**



## Photodiode Noise

k<sub>b</sub> Boltzmann constant 1.38\*10<sup>23</sup>J/K

 $i_j = \sqrt{\frac{4k_b \cdot T_n}{R_{sh}}}$ 

Thermal (Johnson Noise)

Shot noise (dark)

 $i_{sD} = \sqrt{2q \cdot I_D}$ 

Shot noise (w. Light)

$$i_{sL} = \sqrt{2q \cdot I_L}$$

Total Diode Current Noise



**q** Electron Charge 1.6\*10<sup>19</sup> C

T<sub>n</sub> Temperature in Kelvin (25C)

 $\mathbf{f}_{\mathbf{p}}$  Transconductance bandwidth

 $\mathbf{R_{sh}}$  Shunt Resistance in photodiode

ID Dark Current in photodiode

 $I_L$  Photo current in photodiode





## **Noise Gain**

Nodal Analysis on transimpedance amp

$$\frac{V_n}{\frac{1}{s \cdot C_{in}}} + \frac{\left(V_n - V_{out}\right)}{R_f} + \frac{V_n - V_{out}}{\frac{1}{s \cdot C_f}} = 0$$

sRf Vour sC<sub>in</sub> Vn

sCf

Solve for noise gain Vout / Vn

$$\frac{V_{out}}{V_n} = \frac{R_f \cdot (C_f + C_{in}) \cdot s + 1}{C_f \cdot R_f \cdot s + 1}$$

The numerator contains aZero

$$f_{z} = \frac{1}{2\pi R_{f} \cdot (C_{f} + C_{in})}$$

The denominator contains aPole

$$f_{p} = \frac{1}{2\pi R_{f} \cdot C_{f}}$$







## Simulating Noise Gain and Noise Bandwidth



• Break the loop to measure Aol, 1/B, and I to V Gain



### Voltage Noise eni, eno and Eno



**Voltage Noise e**<sub>ni</sub>, e<sub>no</sub> and E<sub>no</sub>  
Region 1 noise: 
$$E_{noe^{1}}^{2} = \int_{f_{t}}^{f_{t}} \frac{e_{nif}^{2} \cdot f_{f}}{f} d_{f} = e_{nif}^{2} f_{f} \ln \frac{f_{f}}{f_{t}}$$
  
Region 2 noise:  $E_{noe^{2}}^{2} = \int_{f_{t}}^{f_{t}} e_{nif}^{2} d_{f} = e_{nif}^{2} (f_{z} - f_{f})$   
Region 3 noise:  $E_{noe^{3}}^{2} = \int_{f_{z}}^{f_{t}} \frac{e_{nif}^{2} \cdot f^{2}}{f_{z}^{2}} d_{f} = \left(\frac{e_{nif}}{f_{z}}\right)^{2} \frac{f_{p}^{3} - f_{z}^{3}}{3}$   
Region 4 noise:  $E_{noe^{4}}^{2} = \int_{f_{p}}^{f_{t}} \left(\frac{e_{nif}}{f}\right)^{2} d_{f} = \left(e_{nif} \cdot \frac{C_{t} + C_{f}}{C_{f}}\right)^{2} (f_{t} - f_{p})$   
Region 5 noise:  $E_{noe^{5}}^{2} = \int_{f_{t}}^{\infty} \left(\frac{e_{nif} f_{c}}{f}\right)^{2} d_{f} = \frac{(e_{nif} f_{c})^{2}}{f_{t}}$   
Total voltage noise:  $E_{noe^{2}}^{2} = E_{noe^{1}}^{2} + E_{noe^{2}}^{2} + E_{noe^{3}}^{2} + E_{noe^{4}}^{2} + E_{noe^{5}}^{2}$ 

## Voltage Noise eni, eno and Eno



## **Resistor Noise and Current Noise**



#### Current noise and resistor noise are limited by the transimpedance (I-V gain) bandwidth

Poles	Kn
1	1.57
2	1.22
3	1.16



## **Bandwidth and Stability**
# **Parasitic Capacitance Limits the Bandwidth**



# **Feedback Capacitance Required for Stability**



# Feedback Capacitance Required for Stability



# **Choosing a Minimum Cf for Stability**



# **Op Amp Calculations**

## **Noise Model for Simple Transimpedance Amp**



## Example Photodiode: PDB-C158

#### ABSOLUTE MAXIMUM RATING (TA)= 23°C UNLESS OTHERWISE NOTED

SYMBOL	PARAMETER	MIN	MAX	UNITS
V <sub>BR</sub>	V <sub>BR</sub> Reverse Voltage		50	V
T <sub>STG</sub>	Storage Temperature	-40	+100	°C
To	Operating Temperature	-40	+80	°C
Ts	Soldering Temperature*		+260	°C

#### SPECTRAL RESPONSE



\* 1/16 inch from case for 3 seconds max.

#### ELECTRO-OPT ICAL CHARACTERISTICS RATING (TA)= 23°C UNLESS OTHERWISE NOTED

	SYMBOL	CHARACTERISTIC	TEST CONDITIONS	MIN	TYP	MAX	UNITS	
	I <sub>SC</sub>	Short Circuit Current	H = 100 fc, 2850 K	100	145		μ <b>A</b>	
	I <sub>D</sub>	Dark Current	V <sub>R</sub> = 10 V		2	30	nA	
•	R <sub>SH</sub>	Sharit Resistance	V <sub>R</sub> = 10 mV	<b>= 100 = </b>	= <b>150</b> = <b>1</b>		■ ■ M 🖳 ■ ■ ■	
	CJ	Junction Capacitance	$V_{R} = 10 V, f = 1 MHz$		10	25	pF	
	= = à range = = :	Spectral Application-Range= = =	•Spot•Sean= = = = = = = = = =	<b>= 400 =</b>		= =1 \$00= =		
-	V <sub>BR</sub>	Breakdown Voltage	I = 10 μA	30	75		V	
	NEP	Noise Equivalent Power	V <sub>R</sub> = 10V @ $\lambda$ = Peak		4.4x10 <sup>-14</sup>		W/ $\sqrt{_{\rm Hz}}$	
	t <sub>r</sub>	Response Time	RL = 1KΩ,V <sub>R</sub> = 10 V		50		nS	

\*\*Response time of 10% to 90% is specified at 660nm wavelength light.

### Cj is not specified at Vr=0V.

Cj=70pF for Vr=0V



# **OPA827** Noise Calculation (key numbers)



# **OPA827** Noise Hand Calculation



## **Poles and Zeros in Noise Gain Curve**



## **Output Noise from OPA Noise Voltage**

$$E_{noe1} \coloneqq \sqrt{e_{nif}^{2} \cdot f_{f} \cdot \ln\left(\frac{f_{f}}{f_{L}}\right)} = 44.573 \times 10^{-9} V$$

$$E_{noe2} \coloneqq \sqrt{e_{nif}^{2} \cdot (f_{z} - f_{f})} = 499.444 \times 10^{-9} V$$

$$E_{noe3} \coloneqq \sqrt{\left(\frac{e_{nif}}{f_{z}}\right)^{2} \cdot \frac{f_{p}^{3} - f_{z}^{3}}{3}} = 31.828 \times 10^{-6} V$$

$$E_{noe4} \coloneqq \sqrt{\left(e_{nif} \cdot \frac{C_{i} + C_{f}}{C_{f}}\right)^{2}} (f_{i} - f_{p}) = 65.324 \times 10^{-6} V$$

$$E_{noe5} \coloneqq \sqrt{\frac{(e_{nif} \cdot f_{c})^{2}}{f_{i}}} = 85.479 \times 10^{-6} V$$

$$E_{noe} \coloneqq \sqrt{E_{noe1}^{2} + E_{noe2}^{2}} + E_{noe3}^{2} + E_{noe4}^{2} + E_{noe5}^{2} = 112.193 \times 10^{-6} V$$





# **Current Noise to Voltage Noise at Output**



## **The Final Total Noise**

 $E_{noe} \approx 112.193 \times 10^{-6} V$  Op-Amp Voltage Noise

 $E_{noR} \approx 32.056 \times 10^{-6} V$ 

**Resistor** Noise

 $E_{noI} \approx 2.17210^{-6} V$ 

**Op-Amp Current Noise** 

 $E_{no} \coloneqq \sqrt{E_{noR}^{2} + E_{noI}^{2} + E_{noe}^{2}} = 116.703 \times 10^{-6} \text{ V}$  Total Output Noise for OPA827 Transimpedance Amp

# **Reducing Noise (Higher Cf = Lower BW Noise)**



# **OPA827 Spice Analysis**

## **OPA827** – test the model



# **Simulated Spectral Density and Total Noise**



# **Op Amp Measurement Example**



## **Validating Test Equipment Capability**



## **Tektronix DPO 4034 Oscilloscope**



 STDEV:
 48uV (same as RMS)

 P-P:
 6.6\*STDEV=319uV

 40s P-P:
 320uV

1) Set DC couple, 20MHz bandwidth limit

2) Short input channel to measure noise floor

# Agilent 4395A Spectrum Analyzer

- 1. Frequency Range: 10Hz~500MHz
- 2. Noise floor: 10nV/rtHz
- **3. Input Impedance:**  $50\Omega$



## **The Noise Floors are Not Good Enough**



# Solution: Use A Post Amp What amp do we Choose?



# OPA847 as post amplifier

Wideband, Ultra-Low Noise, Voltage Feedback, Operational Amplifier







### Post Amplifier Relatively small error!



## **Test the Noise Floor**



# Test The Noise Floor – Post Amp Noise



Simulated	Measured			
(rms)	(rms)			
575uV	518uV			

 STDEV:
 518uV

 P-P:
 6.6\*STDEV=3.4mV

 40s P-P:
 3.88mV



# **Hardware Connections**



- 1. PDB-C158-ND photodiode
- 2. 70pF junction capacitance at Vr=0 V
- 3. 100dB I-V gain
- 4. 4pF compensation capacitor
- 5.  $\pm$  5V power supply.



## **Divide by Gain for OPA827 Output Noise**



# **Measured Spectral Density 4395A Spectrum**



- 1. Agilent 4395A Spectrum
  - Analyzer test 1Hz~20MHz span, 3uV/div, REF=24uV.
- 2. The tested noise density curve shape is the same as

### simulation.



## **OPA827-Noise Density 4395A Spectrum Analyzer**



# Thank you Gen-Probe Staff

- Nick Nickols (AKA S.E Nickols)
- Science.dmr@gmail.com
- 925-256-0161

# References

http://www.radio-electronics.com/info/data/semicond/photo\_diode/structures-materials.php

http://www.rp-photonics.com/photodiodes.html

http://www.rp-photonics.com/photodiodes.html

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http://home.sandiego.edu/~ekim/photodiode/pdtech.html

http://sales.hamamatsu.com/assets/html/ssd/si-photodiode/index.htm

# **Appendix**

http://www.radio-electronics.com/info/data/semicond/photo\_diode/structures-materials.php

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**OPA827** 

www.ti.com

SBOS376F-NOVEMBER 2006-REVISED MARCH 2009

### Low-Noise, High-Precision, JFET-Input OPERATIONAL AMPLIFIER

#### FEATURES

- INPUT VOLTAGE NOISE DENSITY: 4nV/√Hz at 1kHz
- INPUT VOLTAGE NOISE: 0.1Hz to 10Hz: 250nVpp
- INPUT BIAS CURRENT: 15pA
- INPUT OFFSET VOLTAGE: 150μV (max)
- INPUT OFFSET DRIFT: 1.5µV/°C
- GAIN BANDWIDTH: 22MHz
- SLEW RATE: 28V/µs
- QUIESCENT CURRENT: 4.8mA/Ch
- WIDE SUPPLY RANGE: ±4V to ±18V
- PACKAGES: SO-8 and MSOP-8

#### APPLICATIONS

- ADC DRIVERS
- DAC OUTPUT BUFFERS
- TEST EQUIPMENT
- MEDICAL EQUIPMENT
- PLL FILTERS
- SEISMIC APPLICATIONS
- TRANSIMPEDANCE AMPLIFIERS

INPUT VOLTAGE NOISE DENSITY vs FREQUENCY

10

Frequency (Hz)

100

- INTEGRATORS
- ACTIVE FILTERS

F

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0.1

#### DESCRIPTION

The OPA827 series of JFET operational amplifiers combine outstanding dc precision with excellent ac performance. These amplifiers offer low offset voltage (150µV, max), very low drift over temperature (1.5µV/°C, typ), low bias current (15pA, typ), and very low 0.1Hz to 10Hz noise (250nV<sub>PP</sub>, typ). The device operates over a wide supply voltage range, ±4V to ±18V on a low supply current (4.8mA/Ch, typ).

Excellent ac characteristics, such as a 22MHz gain bandwidth product (GBW), a slew rate of 28V/µs, and precision dc characteristics make the OPA827 series well-suited for a wide range of applications including 16-bit to 18-bit mixed signal systems, transimpedance (I/V-conversion) amplifiers, filters, precision ±10V front ends, and professional audio applications.

The OPA827 is available in both SO-8 and MSOP-8 surface-mount packages, and is specified from  $-40^{\circ}$ C to  $+125^{\circ}$ C.



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/o = ±18\

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# **Photodiodes Technologies**

## •<u>Types of photodiodes:</u>

•Although the term photodiode is widely used, there are actually a number of different types of photodiode technologies that can be used.

**<u>PIN photodiode</u>**: This type of photodiode is one of the most widely used forms of photodiode today. Although the PIN or p-i-n photodiode was not the first type of photodiode to be used, it collects the light photons more efficiently than the more standard PN photodiode, and also offers a lower capacitance.(Lot's of application and manufacturers)

<u>*PN photodiode:*</u> The PN photodiode was the first form of photodiode to be developed and used. It is not as widely used as other types which are able to offer better performance parameters. (Solar Cells)

<u>Avalanche photodiode</u>: Avalanche photodiode technology is used in areas of low light. The avalanche photodiode offers very high levels of gain, but against this it has high levels of noise. (Laser range finders)

<u>Schottky photodiode</u>: As the name indicates, Schottky photodiode technology is based upon the Schottky diode. In view of the small diode capacitance it offers a very high speed capability and is used in high bandwidth communication systems.(Telecom/Fiber optics)